Coding challenges

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Exercise 0.1 A peak of an array is an item array[i] such that $array[i] \ge array[i-1]$ and $array[i] \ge array[i+1]$. Note that the first item array[0] is a peak if $array[0] \ge array[1]$ and the last item array[end] is a peak of array if $array[end] \ge array[end-1]$. For instance, L = [2, 1, 4, 3, 7, 9, 10] contains three peaks 2, 4, 10.

Build a function which takes an array of integers and returns a peak. Note that an array contains always a peak and can have many peaks.

Solution: There is a brute-force solution which consists in scanning the array and comparing each item array[i] to array[i-1] and array[i+1]. This solution has a linear time complexity O(N) and O(1) space complexity. (N is the number of the items in the array).

There is another solution which has time complexity $O(\ln N)$ and O(1) space complexity. The idea is to choose the item array[N/2]. Then :

- 1. If array[N/2] \geq array[N/2-1] and array[N/2] \geq array[N/2+1] then array[N/2] is a peak,
- If array[N/2] < array[N/2-1] then you are certain that there is a peak in [array[0],..., array[N/2-1]] and you apply your function to this array,
- 3. If array[N/2] < array[N/2+1] then you are certain that there is a peak in [array[N/2+1],..., array[end]] and you apply your function to this array,

It is a recursive algorithm and the base cases are when N = 1 the function returns the unique item in the array and when N = 2 the function returns the maximum of the array.

